NAG Fortran Library Chapter Contents

F08 - Least-squares and Eigenvalue Problems (LAPACK)

Note: please refer to the Users' Note for your implementation to check that a routine is available.

F08 Chapter Introduction

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Routine Name	Mark of Introduction	Purpose
	inti oduction	•
F08AAF	21	Solves an overdetermined or underdetermined real linear system
F08AEF	16	QR factorization of real general rectangular matrix
F08AFF	16	Form all or part of orthogonal Q from QR factorization determined by
		F08AEF (DGEQRF) or F08BEF (DGEQPF)
F08AGF	16	Apply orthogonal transformation determined by F08AEF (DGEQRF) or F08BEF (DGEQPF)
F08AHF	16	LQ factorization of real general rectangular matrix
F08AJF	16	Form all or part of orthogonal Q from LQ factorization determined by F08AHF (DGELQF)
F08AKF	16	Apply orthogonal transformation determined by F08AHF (DGELQF)
F08ANF	21	Solves an overdetermined or underdetermined complex linear system
F08ASF	16	QR factorization of complex general rectangular matrix
F08ATF	16	Form all or part of unitary Q from QR factorization determined by F08ASF
	- 0	(ZGEQRF) or F08BSF (ZGEQPF)
F08AUF	16	Apply unitary transformation determined by F08ASF (ZGEQRF) or F08BSF (ZGEQPF)
F08AVF	16	LQ factorization of complex general rectangular matrix
F08AWF	16	Form all or part of unitary Q from LQ factorization determined by F08AVF
		(ZGELQF)
F08AXF	16	Apply unitary transformation determined by F08AVF (ZGELQF)
F08BAF	21	Computes the minimum-norm solution to a real linear least-squares problem
F08BEF	16	QR factorization of real general rectangular matrix with column pivoting
F08BFF	21	QR factorization of real general rectangular matrix with column pivoting, using BLAS-3
F08BHF	21	Reduces a real upper trapezoidal matrix to upper triangular form
F08BKF	21	Apply orthogonal transformation determined by F08BHF (DTZRZF)
F08BNF	21	Computes the minimum-norm solution to a complex linear least-squares problem
F08BSF	16	QR factorization of complex general rectangular matrix with column pivoting
F08BTF	21	<i>QR</i> factorization of complex general rectangular matrix with column pivoting,
100011	21	using BLAS-3
F08BVF	21	Reduces a complex upper trapezoidal matrix to upper triangular form
F08BXF	21	Apply unitary transformation determined by F08BVF (ZTZRZF)
F08CEF	21	QL factorization of real general rectangular matrix
F08CFF	21	Form all or part of orthogonal Q from QL factorization determined by F08CEF (DGEQLF)
F08CGF	21	Apply orthogonal transformation determined by F08CEF (DGEQLF)
F08CHF	21	RQ factorization of real general rectangular matrix
F08CJF	21	Form all or part of orthogonal Q from RQ factorization determined by
		F08CHF (DGERQF)
F08CKF	21	Apply orthogonal transformation determined by F08CHF (DGERQF)
F08CSF	21	QL factorization of complex general rectangular matrix
F08CTF	21	Form all or part of orthogonal Q from QL factorization determined by F08CSF (ZGEQLF)
F08CUF	21	Apply unitary transformation determined by F08CSF (ZGEQLF)
F08CVF	21	RQ factorization of complex general rectangular matrix

F08CWF	21	Form all or part of orthogonal Q from RQ factorization determined by F08CVF (ZGERQF)
F08CXF	21	Apply unitary transformation determined by F08CVF (ZGERQF)
F08FAF	21	Computes all eigenvalues and, optionally, eigenvectors of a real symmetric
1 001711	21	matrix
EOGEDE	21	
F08FBF	21	Computes selected eigenvalues and, optionally, eigenvectors of a real
		symmetric matrix
F08FCF	19	All eigenvalues and optionally all eigenvectors of real symmetric matrix
		(divide-and-conquer)
F08FDF	21	Computes selected eigenvalues and, optionally, eigenvectors of a real
		symmetric matrix (Relatively Robust Representations)
F08FEF	16	Orthogonal reduction of real symmetric matrix to symmetric tridiagonal form
F08FFF	16	Generate orthogonal transformation matrix from reduction to tridiagonal form
		determined by F08FEF (DSYTRD)
F08FGF	16	Apply orthogonal transformation determined by F08FEF (DSYTRD)
F08FLF	21	Computes the reciprocal condition numbers for the eigenvectors of a real
TOOTLI	21	
		symmetric or complex Hermitian matrix or for the left or right singular
EGGENIE	2.1	vectors of a general matrix
F08FNF	21	Computes all eigenvalues and, optionally, eigenvectors of a complex
		Hermitian matrix
F08FPF	21	Computes selected eigenvalues and, optionally, eigenvectors of a complex
		Hermitian matrix
F08FQF	19	All eigenvalues and optionally all eigenvectors of complex Hermitian matrix
		(divide-and-conquer)
F08FRF	21	Computes selected eigenvalues and, optionally, eigenvectors of a complex
		Hermitian matrix (Relatively Robust Representations)
F08FSF	16	Unitary reduction of complex Hermitian matrix to real symmetric tridiagonal
1 001 51	10	form
F08FTF	16	Generate unitary transformation matrix from reduction to tridiagonal form
1.001, 11,	10	determined by F08FSF (ZHETRD)
F08FUF	16	Apply unitary transformation matrix determined by F08FSF (ZHETRD)
F08GAF	21	Computes all eigenvalues and, optionally, eigenvectors of a real symmetric
EOOCDE	21	matrix, packed storage
F08GBF	21	Computes selected eigenvalues and, optionally, eigenvectors of a real
E00000	10	symmetric matrix, packed storage
F08GCF	19	All eigenvalues and optionally all eigenvectors of real symmetric matrix,
		packed storage (divide-and-conquer)
F08GEF	16	Orthogonal reduction of real symmetric matrix to symmetric tridiagonal form,
		packed storage
F08GFF	16	Generate orthogonal transformation matrix from reduction to tridiagonal form
		determined by F08GEF (DSPTRD)
F08GGF	16	Apply orthogonal transformation determined by F08GEF (DSPTRD)
F08GNF	21	Computes all eigenvalues and, optionally, eigenvectors of a complex
		Hermitian matrix, packed storage
F08GPF	21	Computes selected eigenvalues and, optionally, eigenvectors of a complex
100011	21	Hermitian matrix, packed storage
F08GQF	19	All eigenvalues and optionally all eigenvectors of complex Hermitian matrix,
rooder	19	packed storage (divide-and-conquer)
EOOCCE	1.6	
F08GSF	16	Unitary reduction of complex Hermitian matrix to real symmetric tridiagonal
EGGGEE	1.6	form, packed storage
F08GTF	16	Generate unitary transformation matrix from reduction to tridiagonal form
		determined by F08GSF (ZHPTRD)
F08GUF	16	Apply unitary transformation matrix determined by F08GSF (ZHPTRD)
F08HAF	21	Computes all eigenvalues and, optionally, eigenvectors of a real symmetric
		band matrix
F08HBF	21	Computes selected eigenvalues and, optionally, eigenvectors of a real
		symmetric band matrix
F08HCF	19	All eigenvalues and optionally all eigenvectors of real symmetric band matrix
- -	-	(divide-and-conquer)
		,

F08HEF	16	Orthogonal reduction of real symmetric band matrix to symmetric tridiagonal form
F08HNF	21	Computes all eigenvalues and, optionally, eigenvectors of a complex Hermitian band matrix
F08HPF	21	Computes selected eigenvalues and, optionally, eigenvectors of a complex
F08HQF	19	Hermitian band matrix All eigenvalues and optionally all eigenvectors of complex Hermitian band
F08HSF	16	matrix (divide-and-conquer) Unitary reduction of complex Hermitian band matrix to real symmetric
F08JAF	21	tridiagonal form Computes all eigenvalues and, optionally, eigenvectors of a real symmetric
		tridiagonal matrix
F08JBF	21	Computes selected eigenvalues and, optionally, eigenvectors of a real symmetric tridiagonal matrix
F08JCF	19	All eigenvalues and optionally all eigenvectors of real symmetric tridiagonal matrix (divide-and-conquer)
F08JDF	21	Computes selected eigenvalues and, optionally, eigenvectors of a real symmetric tridiagonal matrix (Relatively Robust Representations)
F08JEF	16	All eigenvalues and eigenvectors of real symmetric tridiagonal matrix, reduced from real symmetric matrix using implicit <i>QL</i> or <i>QR</i>
F08JFF	16	All eigenvalues of real symmetric tridiagonal matrix, root-free variant of QL
F08JGF	16	or <i>QR</i> All eigenvalues and eigenvectors of real symmetric positive-definite
F08JHF	21	tridiagonal matrix, reduced from real symmetric positive-definite matrix Computes all eigenvalues and, optionally, eigenvectors of a real symmetric
F08JJF	16	tridiagonal matrix or a matrix reduced to this form (divide-and-conquer) Selected eigenvalues of real symmetric tridiagonal matrix by bisection
F08JKF	16	Selected eigenvectors of real symmetric tridiagonal matrix by inverse iteration, storing eigenvectors in real array
F08JLF	21	Computes all eigenvalues and, optionally, eigenvectors of a real symmetric tridiagonal matrix or a symmetric matrix reduced to this form (Relatively Robust Representations)
F08JSF	16	All eigenvalues and eigenvectors of real symmetric tridiagonal matrix, reduced from complex Hermitian matrix, using implicit <i>QL</i> or <i>QR</i>
F08JUF	16	All eigenvalues and eigenvectors of real symmetric positive-definite
F08JVF	21	tridiagonal matrix, reduced from complex Hermitian positive-definite matrix Computes all eigenvalues and, optionally, eigenvectors of a real symmetric
		tridiagonal matrix or a complex Hermitian matrix reduced to this form (divide-and-conquer)
F08JXF	16	Selected eigenvectors of real symmetric tridiagonal matrix by inverse iteration, storing eigenvectors in complex array
F08JYF	21	Computes all eigenvalues and, optionally, eigenvectors of a real symmetric
		tridiagonal matrix or a complex Hermitian matrix reduced to this form (Relatively Robust Representations)
F08KAF	21	Computes the minimum-norm solution to a real linear least-squares problem using singular value decomposition
F08KBF	21	Computes the singular value decomposition of a real matrix, optionally
F08KCF	21	computing the left and/or right singular vectors Computes the minimum-norm solution to a real linear least-squares problem
F08KDF	21	using singular value decomposition (divide-and-conquer) Computes the singular value decomposition of a real matrix, optionally
		computing the left and/or right singular vectors (divide-and-conquer)
F08KEF	16	Orthogonal reduction of real general rectangular matrix to bidiagonal form
F08KFF	16	Generate orthogonal transformation matrices from reduction to bidiagonal form determined by F08KEF (DGEBRD)
F08KGF	16	Apply orthogonal transformations from reduction to bidiagonal form determined by F08KEF (DGEBRD)
F08KNF	21	Computes the minimum-norm solution to a complex linear least-squares problem using singular value decomposition

F08KPF	21	Computes the singular value decomposition of a complex matrix, optionally computing the left and/or right singular vectors
F08KQF	21	Computes the minimum-norm solution to a complex linear least-squares
EOOKBE	0.1	problem using singular value decomposition (divide-and-conquer)
F08KRF	21	Computes the singular value decomposition of a complex matrix, optionally computing the left and/or right singular vectors (divide-and-conquer)
F08KSF	16	Unitary reduction of complex general rectangular matrix to bidiagonal form
F08KTF	16	Generate unitary transformation matrices from reduction to bidiagonal form
		determined by F08KSF (ZGEBRD)
F08KUF	16	Apply unitary transformations from reduction to bidiagonal form determined by F08KSF (ZGEBRD)
F08LEF	19	Reduction of real rectangular band matrix to upper bidiagonal form
F08LSF	19	Reduction of complex rectangular band matrix to upper bidiagonal form
F08MDF	21	Computes the singular value decomposition of a real bidiagonal matrix,
FOOMEE	1.6	optionally computing the singular vectors (divide-and-conquer)
F08MEF	16	SVD of real bidiagonal matrix reduced from real general matrix
F08MSF	16	SVD of real bidiagonal matrix reduced from complex general matrix
F08NAF	21	Computes all eigenvalues and, optionally, left and/or right eigenvectors of a real nonsymmetric matrix
F08NBF	21	Computes all eigenvalues and, optionally, left and/or right eigenvectors of a real nonsymmetric matrix; also, optionally, the balancing transformation, the
		reciprocal condition numbers for the eigenvalues and for the right
FOONER	1.6	eigenvectors
F08NEF	16	Orthogonal reduction of real general matrix to upper Hessenberg form
F08NFF	16	Generate orthogonal transformation matrix from reduction to Hessenberg form determined by F08NEF (DGEHRD)
F08NGF	16	Apply orthogonal transformation matrix from reduction to Hessenberg form determined by F08NEF (DGEHRD)
F08NHF	16	Balance real general matrix
F08NJF	16	Transform eigenvectors of real balanced matrix to those of original matrix
		supplied to F08NHF (DGEBAL)
F08NNF	21	Computes all eigenvalues and, optionally, left and/or right eigenvectors of a complex nonsymmetric matrix
F08NPF	21	Computes all eigenvalues and, optionally, left and/or right eigenvectors of a
		complex nonsymmetric matrix; also, optionally, the balancing transformation, the reciprocal condition numbers for the eigenvalues and for the right
		eigenvectors
F08NSF F08NTF	16 16	Unitary reduction of complex general matrix to upper Hessenberg form Generate unitary transformation matrix from reduction to Hessenberg form
		determined by F08NSF (ZGEHRD)
F08NUF	16	Apply unitary transformation matrix from reduction to Hessenberg form determined by F08NSF (ZGEHRD)
F08NVF	16	Balance complex general matrix
F08NWF	16	Transform eigenvectors of complex balanced matrix to those of original
LOON WI	10	matrix supplied to F08NVF (ZGEBAL)
F08PAF	21	Computes for real square nonsymmetric matrix, the eigenvalues, the real
		Schur form, and, optionally, the matrix of Schur vectors
F08PBF	21	Computes for real square nonsymmetric matrix, the eigenvalues, the real Schur form, and, optionally, the matrix of Schur vectors; also, optionally,
EAODEE	1.6	computes reciprocal condition numbers for selected eigenvalues
F08PEF	16	Eigenvalues and Schur factorization of real upper Hessenberg matrix reduced from real general matrix
F08PKF	16	Selected right and/or left eigenvectors of real upper Hessenberg matrix by inverse iteration
F08PNF	21	Computes for complex square nonsymmetric matrix, the eigenvalues, the
I OOI IVI	<i>L</i> 1	Schur form, and, optionally, the matrix of Schur vectors
F08PPF	21	Computes for real square nonsymmetric matrix, the eigenvalues, the Schur
		form, and, optionally, the matrix of Schur vectors; also, optionally, computes
		reciprocal condition numbers for selected eigenvalues

F08PSF	16	Eigenvalues and Schur factorization of complex upper Hessenberg matrix reduced from complex general matrix
F08PXF	16	Selected right and/or left eigenvectors of complex upper Hessenberg matrix by inverse iteration
F08QFF	16	Reorder Schur factorization of real matrix using orthogonal similarity transformation
F08QGF	16	Reorder Schur factorization of real matrix, form orthonormal basis of right invariant subspace for selected eigenvalues, with estimates of sensitivities
F08QHF	16	Solve real Sylvester matrix equation $AX + XB = C$, A and B are upper quasitriangular or transposes
FOOOME	1.6	
F08QKF	16	Left and right eigenvectors of real upper quasi-triangular matrix
F08QLF	16	Estimates of sensitivities of selected eigenvalues and eigenvectors of real upper quasi-triangular matrix
F08QTF	16	Reorder Schur factorization of complex matrix using unitary similarity transformation
F08QUF	16	Reorder Schur factorization of complex matrix, form orthonormal basis of
100001	10	right invariant subspace for selected eigenvalues, with estimates of sensitivities
F08QVF	16	Solve complex Sylvester matrix equation $AX + XB = C$, A and B are upper triangular or conjugate-transposes
F08QXF	16	Left and right eigenvectors of complex upper triangular matrix
F08QYF	16	Estimates of sensitivities of selected eigenvalues and eigenvectors of complex
100011	10	upper triangular matrix
F08SAF	21	Computes all the eigenvalues, and optionally, the eigenvectors of a real
1'005A1'	21	
FOOCDE	21	generalized symmetric-definite eigenproblem
F08SBF	21	Computes selected eigenvalues, and optionally, the eigenvectors of a real
		generalized symmetric-definite eigenproblem
F08SCF	21	Computes all the eigenvalues, and optionally, the eigenvectors of a real
		generalized symmetric-definite eigenproblem (divide-and-conquer)
F08SEF	16	Reduction to standard form of real symmetric-definite generalized eigenproblem $Ax = \lambda Bx$, $ABx = \lambda x$ or $BAx = \lambda x$, B factorized by F07FDF (DPOTRF)
F08SNF	21	Computes all the eigenvalues, and optionally, the eigenvectors of a complex generalized Hermitian-definite eigenproblem
EOCCDE	21	
F08SPF	21	Computes selected eigenvalues, and optionally, the eigenvectors of a complex generalized Hermitian-definite eigenproblem
F08SQF	21	Computes all the eigenvalues, and optionally, the eigenvectors of a complex generalized Hermitian-definite eigenproblem (divide-and-conquer)
F08SSF	16	Reduction to standard form of complex Hermitian-definite generalized
		eigenproblem $Ax = \lambda Bx$, $ABx = \lambda x$ or $BAx = \lambda x$, B factorized by F07FRF
		(ZPOTRF)
F08TAF	21	Computes all the eigenvalues, and optionally, the eigenvectors of a real
		generalized symmetric-definite eigenproblem, packed storage
F08TBF	21	Computes selected eigenvalues, and optionally, the eigenvectors of a real
		generalized symmetric-definite eigenproblem, packed storage
F08TCF	21	Computes all the eigenvalues, and optionally, the eigenvectors of a real
		generalized symmetric-definite eigenproblem, packed storage (divide-and-
		conquer)
F08TEF	16	Reduction to standard form of real symmetric-definite generalized
		eigenproblem $Ax = \lambda Bx$, $ABx = \lambda x$ or $BAx = \lambda x$, packed storage, B factorized
		by F07GDF (DPPTRF)
F08TNF	21	Computes all the eigenvalues, and optionally, the eigenvectors of a complex
LOGITM	<i>L</i> 1	
EASTRE	21	generalized Hermitian-definite eigenproblem, packed storage
F08TPF	21	Computes selected eigenvalues, and optionally, the eigenvectors of a complex
E00=0=	2.4	generalized Hermitian-definite eigenproblem, packed storage
F08TQF	21	Computes selected eigenvalues, and optionally, the eigenvectors of a complex
		generalized Hermitian-definite eigenproblem, packed storage (divide-and-
		conquer)

F00F0F	4.6	
F08TSF	16	Reduction to standard form of complex Hermitian-definite generalized
		eigenproblem $Ax = \lambda Bx$, $ABx = \lambda x$ or $BAx = \lambda x$, packed storage, B factorized by F07GRF (ZPPTRF)
F08UAF	21	Computes all the eigenvalues, and optionally, the eigenvectors of a real
		banded generalized symmetric-definite eigenproblem
F08UBF	21	Computes selected eigenvalues, and optionally, the eigenvectors of a real
		banded generalized symmetric-definite eigenproblem
F08UCF	21	Computes all the eigenvalues, and optionally, the eigenvectors of a real
FACTIFF	10	banded generalized symmetric-definite eigenproblem (divide-and-conquer)
F08UEF	19	Reduction of real symmetric-definite banded generalized eigenproblem
		$Ax = \lambda Bx$ to standard form $Cy = \lambda y$, such that C has the same bandwidth as A
F08UFF	19	Computes a split Cholesky factorization of real symmetric positive-definite
100011	17	band matrix A
F08UNF	21	Computes all the eigenvalues, and optionally, the eigenvectors of a complex
		banded generalized Hermitian-definite eigenproblem
F08UPF	21	Computes selected eigenvalues, and optionally, the eigenvectors of a complex
		banded generalized Hermitian-definite eigenproblem
F08UQF	21	Computes all the eigenvalues, and optionally, the eigenvectors of a complex
EOOLIGE	19	banded generalized Hermitian-definite eigenproblem (divide-and-conquer) Reduction of complex Hermitian-definite banded generalized eigenproblem
F08USF	19	$Ax = \lambda Bx$ to standard form $Cy = \lambda y$, such that C has the same bandwidth as
		A
F08UTF	19	Computes a split Cholesky factorization of complex Hermitian positive-
		definite band matrix A
F08VAF	21	Computes the generalized singular value decomposition of a real matrix pair
F08VEF	21	Computes orthogonal matrices as processing steps for computing the
EOOVAJE	2.1	generalized singular value decomposition of a real matrix pair
F08VNF	21	Computes the generalized singular value decomposition of a complex matrix pair
F08VSF	21	Computes orthogonal matrices as processing steps for computing the
100 (51	21	generalized singular value decomposition of a complex matrix pair
F08WAF	21	Computes, for a real nonsymmetric matrix pair, the generalized eigenvalues,
		and optionally, the left and/or right generalized eigenvectors
F08WBF	21	Computes, for a real nonsymmetric matrix pair, the generalized eigenvalues,
		and optionally, the left and/or right generalized eigenvectors; also, optionally,
		the balancing transformation, the reciprocal condition numbers for the
F08WEF	20	eigenvalues and for the right eigenvectors Orthogonal reduction of a pair of real general matrices to generalized upper
1 00 W L1	20	Hessenberg form
F08WHF	20	Balance a pair of real general matrices
F08WJF	20	Transform eigenvectors of a pair of real balanced matrices to those of original
		matrix pair supplied to F08WHF (DGGBAL)
F08WNF	21	Computes, for a complex nonsymmetric matrix pair, the generalized
FOOMBE	21	eigenvalues, and optionally, the left and/or right generalized eigenvectors
F08WPF	21	Computes, for a complex nonsymmetric matrix pair, the generalized eigenvalues, and optionally, the left and/or right generalized eigenvectors;
		also, optionally, the balancing transformation, the reciprocal condition
		numbers for the eigenvalues and for the right eigenvectors
F08WSF	20	Unitary reduction of a pair of complex general matrices to generalized upper
		Hessenberg form
F08WVF	20	Balance a pair of complex general matrices
F08WWF	20	Transform eigenvectors of a pair of complex balanced matrices to those of
EOOXAE	0.1	original matrix pair supplied to F08WVF (ZGGBAL)
F08XAF	21	Computes, for a real nonsymmetric matrix pair, the generalized eigenvalues, the generalized real Schur form and, optionally, the left and/or right matrices
		of Schur vectors
		- 20 / 2000

selected eigenvalues Eigenvalues and generalized Schur factorization of real generalized upper Hessenberg form reduced from a pair of real general matrices F08XNF 21 Computes, for a complex nonsymmetric matrix pair, the generalized eigenvalues, the generalized complex Schur form and, optionally, the left and/ or right matrices of Schur vectors F08XPF 21 Computes, for a complex nonsymmetric matrix pair, the generalized eigenvalues, the generalized complex Schur form and, optionally, the left and/ or right matrices of Schur vectors; also, optionally, computes reciprocal condition numbers for selected eigenvalues F08XSF 20 Eigenvalues and generalized Schur factorization of complex generalized upper Hessenberg form reduced from a pair of complex general matrices F08YFF 21 Computes the generalized singular value decomposition of a real matrix pair using an orthogonal equivalence transformation F08YGF 21 Reorders the generalized real Schur decomposition of a real matrix pair using an orthogonal equivalence transformation, computes the generalized eigenvalues of the reordered pair and, optionally, computes the estimates of reciprocal condition numbers for eigenvalues and eigenspaces F08YHF 21 Solves the real-valued generalized Sylvester equation F08YGF 22 Left and right eigenvectors of a pair of real upper quasi-triangular matrices Estimates reciprocal condition numbers for specified eigenvalues and/or eigenvectors of a real matrix pair in generalized real Schur canonical form or eigenvectors of a real matrix pair in generalized real Schur canonical form F08YGF 21 Computes the generalized Schur decomposition of a complex upper triangular (or trapezoidal) matrix pair F08YFF 21 Reorders the generalized Schur decomposition of a complex matrix pair using an unitary equivalence transformation, computes the generalized eigenvalues of the reordered pair and, optionally, computes the estimates of reciprocal condition numbers for specified eigenvalues and/or eigenvectors for a pair of complex matrix pair usin	F08XBF	21	Computes, for a real nonsymmetric matrix pair, the generalized eigenvalues, the generalized real Schur form and, optionally, the left and/or right matrices of Schur vectors; also, optionally, computes reciprocal condition numbers for
FO8XNF 21 Computes, for a complex nonsymmetric matrix pair, the generalized eigenvalues, the generalized complex Schur form and, optionally, the left and/ or right matrices of Schur vectors FO8XNF 21 Computes, for a complex nonsymmetric matrix pair, the generalized eigenvalues, the generalized complex Schur form and, optionally, the left and/ or right matrices of Schur vectors; also, optionally, computes reciprocal condition numbers for selected eigenvalues FO8XSF 20 Eigenvalues and generalized Schur factorization of complex generalized upper Hessenberg form reduced from a pair of complex general matrices FO8YFF 21 Reorders the generalized singular value decomposition of a real upper triangular (or trapezoidal) matrix pair FO8YFF 21 Reorders the generalized real Schur decomposition of a real matrix pair using an orthogonal equivalence transformation, computes the generalized eigenvalues of the reordered pair and, optionally, computes the estimates of reciprocal condition numbers for eigenvalues and eigenspaces FO8YHF 21 Reorders the real-valued generalized Sylvester equation FO8YLF 20 Left and right eigenvectors of a pair of real upper quasi-triangular matrices FO8YLF 21 Estimates reciprocal condition numbers for specified eigenvalues and/or eigenvectors of a real matrix pair in generalized requation FO8YFF 21 Computes the generalized singular value decomposition of a complex upper triangular (or trapezoidal) matrix pair FO8YTF 21 Reorders the generalized Schur decomposition of a complex matrix pair using an unitary equivalence transformation. computes the generalized eigenvalues of the reordered pair and, optionally, computes the generalized eigenvalues of the reordered pair and, optionally, computes the generalized eigenvalues of the reordered pair and, optionally, computes the estimates of reciprocal condition numbers for eigenvalues and eigenspaces FO8YVF 21 Solves the complex generalized Schur decomposition of a complex matrix pair using an unitary equivalence transformation computes the estimate	F08XEF	20	Eigenvalues and generalized Schur factorization of real generalized upper
F08XFF 21 Computes, for a complex nonsymmetric matrix pair, the generalized eigenvalues, the generalized complex Schur form and, optionally, the left and/ or right matrices of Schur vectors; also, optionally, computes reciprocal condition numbers for selected eigenvalues F08XFF 20 Eigenvalues and generalized Schur factorization of complex generalized upper Hessenberg form reduced from a pair of complex general matrices F08YFF 21 Reorders the generalized singular value decomposition of a real upper triangular (or trapezoidal) matrix pair F08YGF 21 Reorders the generalized real Schur decomposition of a real matrix pair using an orthogonal equivalence transformation F08YGF 21 Reorders the generalized real Schur decomposition of a real matrix pair using an orthogonal equivalence transformation, computes the generalized eigenvalues of the reordered pair and, optionally, computes the estimates of reciprocal condition numbers for eigenvalues and eigenspaces F08YHF 20 Left and right eigenvectors of a pair of real upper quasi-triangular matrices F08YFF 21 Estimates reciprocal condition numbers for specified eigenvalues and/or eigenvectors of a real matrix pair in generalized real Schur canonical form F08YFF 21 Computes the generalized Singular value decomposition of a complex upper triangular (or trapezoidal) matrix pair F08YFF 21 Reorders the generalized Schur decomposition of a complex matrix pair using an unitary equivalence transformation F08YUF 21 Reorders the generalized Schur decomposition of a complex matrix pair using an unitary equivalence transformation, computes the generalized eigenvalues of the reordered pair and, optionally, computes the generalized eigenvalues of the reordered pair and, optionally, computes the estimates of reciprocal condition numbers for eigenvalues and eigenspaces F08YVF 21 Solves the complex matrix pair in generalized Schur canonical form eigenvectors of a complex matrix pair perior eigenvectors of a complex matrix pair in generalized Schur canonical form Solves a real gene	F08XNF	21	Computes, for a complex nonsymmetric matrix pair, the generalized eigenvalues, the generalized complex Schur form and, optionally, the left and/
F08XSF 21 Eigenvalues and generalized Schur factorization of complex generalized upper Hessenberg form reduced from a pair of complex general matrices F08YFF 21 Computes the generalized singular value decomposition of a real upper triangular (or trapezoidal) matrix pair F08YGF 21 Reorders the generalized real Schur decomposition of a real matrix pair using an orthogonal equivalence transformation F08YGF 21 Reorders the generalized real Schur decomposition of a real matrix pair using an orthogonal equivalence transformation, computes the generalized eigenvalues of the reordered pair and, optionally, computes the estimates of reciprocal condition numbers for eigenvalues and eigenspaces F08YHF 21 Solves the real-valued generalized Sylvester equation F08YKF 20 Left and right eigenvectors of a pair of real upper quasi-triangular matrices F08YLF 21 Estimates reciprocal condition numbers for specified eigenvalues and/or eigenvectors of a real matrix pair in generalized real Schur canonical form F08YSF 21 Computes the generalized singular value decomposition of a complex upper triangular (or trapezoidal) matrix pair F08YUF 21 Reorders the generalized Schur decomposition of a complex matrix pair using an unitary equivalence transformation F08YVF 21 Reorders the generalized Schur decomposition of a complex matrix pair using an unitary equivalence transformation, computes the generalized eigenvalues of the reordered pair and, optionally, computes the generalized eigenvalues of the reordered pair and, optionally, computes the generalized of the reordered pair and, optionally, computes the generalized of the reordered pair and, optionally computes the generalized of the reordered pair and, optionally computes the generalized of the reordered pair and, optionally computes the generalized of the reordered pair and, optionally computes the generalized of the reordered pair and, optionally computes the generalized of the reordered pair and, optionally computes the generalized of the reordered pair and, optionally computes the g	F08XPF	21	Computes, for a complex nonsymmetric matrix pair, the generalized eigenvalues, the generalized complex Schur form and, optionally, the left and/ or right matrices of Schur vectors; also, optionally, computes reciprocal
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